Invariant Moment Based ID3 Classifier for Face Recognition Satya Sreedevi Redla, Dr. Vamsi Krishna Mangalampalli, Dr. Banitamani Mallik

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Abstract- The biometric-based face recognition techniques are considered to be most promising methods in face recognition systems. Many different methods of capturing features of facial image and compare with those images in database have been proposed in last few decades. The challenges in recognition system due to different imaging conditions in real-world like illuminations, expressions, poses and faces with low-resolution made researchers to continue to develop new methods to reduce the huge volumes of data, to increase the efficiency and accuracy of recognition process. This paper develops face recognition methodology based on 7 Hu moments invariant of rotation, translation & scaling and ID3 classifier. Methodology and demonstrations are being provided on Bio id face benchmark data base as proof of concept. It is noticed 91% accuracy is attained on randomly selected sample of 10 individual's faces.

Keywords: Face Recognition, Face detection, Feature extraction, Hu moments, ID3 classifier

INTRODUCTION

In 1960s the first semi-automated system for facial recognition was carried out manually to locate the features like eyes, ears, nose and mouth on the photographs before it calculated ratios and distance to a common reference point. These features were then compared to a reference data base. In 1970 Goldstein and Harmon used 21 specific subjective points such as hair color, lip thickness etc. to automate the face recognition. In 1988, Kirby and Sirovich applied Principal component analysis and a standard linear algebra technique to compress the face images. In 1991, Turk and Pentland [2] discovered that while using eigenfaces technique, the residual errors can be used to detect faces in images for a reliable real time automated face recognition system.

The face recognition system procedure consists of Face Detection, Feature Extraction, and Face Recognition [1].

A work flow of image-based face recognition system proposed by Wei-Lun Chao depicted in the Fig 1.



Fig 1: General face recognition system

Face detection is to identify an object as a face in the input image. we first check whether human faces appear in the input image and then find the location of these faces in the image.

After the human-faces are extracted from image. We cannot use directly these faces in recognition system because of certain problems like dimensionality (For example, the dimensionality of each face vector of 512X512 image is 250,000), camera alignments, different facial expressions, illuminations, and may suffer from occlusion and clutter. To overcome these drawbacks, feature extractions are performed. A feature is a piece of information that describes an image or part of an image. Size of the feature and the number of features extracted from a single facial image are significant in system.

After extracting features, w to decide whether the input image is known or unknown based on database of faces.

In Face identification we want the recognition system to tell who it is from a given image; while in face verification, given a face image and a guess of identification, we want the system to tell true or false about the guess.

A questioned image will be pre-processed and a region of interest will be fetched from that image. It is then, submitted to the face recognition system. This paper assumes that the given questioned image as whole is a region of interest. Hence this paper is not considering the pre-processing stage. Also, the questioned image may be in different orientation, which will have an influence on the face recognition.

The present study considers 7 HU moments which were invariant with respect to rotation, translation and scaling [6], [7]. A brief account of this is provided in section II for completeness.

In [7], the Hu central moments of the image function f(x,y) with p as the order of x and q as the of y is defined as

(1)

$$\mu_{pq} = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} (x - \overline{x})^p (y - \overline{y})^q f(x, y) dx dy$$

$$p, q = 0, 1, 2, \cdots$$
ere
$$\overline{x} = \frac{m_{10}}{y} = \frac{m_{01}}{y}$$

 m_{00}

Scale invariance can be obtained by normalization. The normalized central moments are defined as

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 m_{00}

wh

$$\eta_{pq} = \frac{\mu_{pq}}{\mu_{00}^{\gamma}}, \ \gamma = (p+q+2)/2, \ p+q=2,3,\cdots$$

(2)

Based on the normalized central moments, Hu introduced seven moment invariants. These seven moment invariants are unchanged under image scaling, translation and rotation are

$$\begin{split} \phi_{1} &= \eta_{20} + \eta_{02} \\ \phi_{2} &= (\eta_{20} - \eta_{02})^{2} + 4\eta_{11}^{2} \\ \phi_{3} &= (\eta_{30} - 3\eta_{12})^{2} + (3\eta_{21} - \mu_{03})^{2} \\ \phi_{4} &= (\eta_{30} + \eta_{12})^{2} + (\eta_{21} + \mu_{03})^{2} \\ \phi_{5} &= (\eta_{30} - 3\eta_{12})(\eta_{30} + \eta_{12})[(\eta_{30} + \eta_{12})^{2} - 3(\eta_{21} + \eta_{03})^{2}] \\ &+ (3\eta_{21} - \eta_{03})(\eta_{21} + \eta_{03}](3(\eta_{30} + \eta_{12})^{2} - (\eta_{21} + \eta_{03})^{2}] \\ \phi_{6} &= (\eta_{20} - \eta_{02})[(\eta_{30} + \eta_{12})^{2} - (\eta_{21} + \eta_{03})^{2}] \\ &+ 4\eta_{11}(\eta_{30} + \eta_{12})(\eta_{21} + \eta_{03}) \\ \phi_{7} &= (3\eta_{21} - \eta_{03})(\eta_{30} + \eta_{12})[(\eta_{30} + \eta_{12})^{2} - 3(\eta_{21} + \eta_{03})^{2}] \\ &- (\eta_{30} - 3\eta_{12})(\eta_{21} + \eta_{03})[(3(\eta_{30} + \eta_{12})^{2} - (\eta_{21} + \eta_{03})^{2}] \\ \end{split}$$
(3)

The following section of this paper provides feature extraction from the given image and the corresponding illustration. Mean, SD, CV and 7 invariant moments are considered as features and be computed for the given images. The individual person id of the image is labeled as class. The Data is divided into two parts. One will be training part and the other will be testing part. Data preparation is explained in section II along with statistics.

In this paper a ID3 classifier has been built in Matlab by using training data set. The performance of the model is tested on the test data set.

Bio id face benchmark data base is considered for the demonstration of the proposed methodology. Rest of the paper as follows

2. DATA PREPARATION & PROPOSED METHODOLOGY

Ten features namely Mean, SD, CV and 7 invariant moments for each image were computed as a real vector of size 10. A class label is the person id of the image and it is a categorical data type. Thus each image is represented by a vector of 10 real numbers with one categorical data item. Fig 2 is the given image for which the features are computed and represented as vector as shown below.



Fig2: A Given image (S_id 180)

Mean = 107.5078 SD= 67.10222 IM3= 2.39E-11 IM4=1.41E-11

| CV= 62.41611 | IM5=1.63E-22 |
|---------------|---------------|
| IM1 =0.001377 | IM6=-6E-15 |
| IM2= 1.84E-07 | IM7= 3.91E-23 |

Bio Id Face Database: This dataset consists of 1521 gray level images with a resolution of 384x286 pixel of different individuals with different frequencies. The Database was recorded and published for the researchers to work in the area of face detection and to compare the quality of their algorithms with others. During the recording the images a special emphasis has been laid on "real world" conditions. Therefore, the test set features a large variety of illumination, background and face size. For sample images please visit the BioID Face DB page.

Images pertaining to 10 individuals with reasonable frequency has been selected for demonstration purpose. Hence the data set consist of 445 images of 10 individuals with ids 180, 260, 322, 418, 449, 483, 519, 660, 741, and 973. A sample image of each of 10 individuals is given in the following Fig 3 and their labelled ids in table I

| S_id: | 180 | 260 | 322 | 418 | 449 | 483 | 519 | 660 | 741 | 973 | | | |
|-------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|--|-----|-----|
| 180 | | | | 260 | | | | 322 | | | | 418 | 449 |
| | | | | | | | | 6 | | | | | Ø. |
| 483 | | | | 519 | | | | 660 | | | | 741 | 973 |
| | | | | | | | | | | | | | |

Table I: Selected Persons Ids (S_id)

Fig 3:Sample faces of Selected 10 individuals corresponding to Table I

In Table II, ISNo represents the image id, S id represents the person id, mean, SD, CV, IM1, IM2, IM3, IM5, IM6 and IM7 are the features of these 10 individuals and Class is nothing but S_id.

The following provides a sample of 6 images of an individual labelled as 180 as shown in Fig 4.





Fig 4: A sample six faces of person S_id =180

The Box plots of the 6 image in Fig4 is given in Fig 5 respectively. These Box plots displays range and distribution of data along the number line.



Fig 5: Box Plots corresponds the image data given in fig4

Analysing the box plots, one can notice variation in the plots corresponds to 6 images of the same individual. This challenges the face recognition system.

The composition of 445 images in our demonstrative data base related to 10 individuals is in Table III

| S_id | Number of Images |
|------|------------------|
| 180 | 42 |
| 260 | 48 |
| 322 | 92 |
| 418 | 31 |

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| 449 | 33 |
|-----|----|
| 483 | 36 |
| 519 | 37 |
| 660 | 46 |
| 741 | 38 |
| 973 | 42 |

Table III: Representation of faces of the selected 10 individuals in the demonstrative Data set of size 445

The abstract aspect of the features of the 445 images is given in the Table IV and Table V. The average of the 10 features listed in table IV and Standard deviation of the 10 features in Table V respectively.

Histogram of all the 10 features of the selected data set is provided in Fig



Fig 6: Histograms of the Features of Data Set

3. PERFORMANCE OF PROPOSED METHODOLOGY IVMID3

The given images are divided into Training and Testing Image Sets. The considered 445 Images of Bio Id face bench mark data set are divided into training and testing data sets with sizes 299 and 146 respectively by maintaining proper representation of each individual.

The corresponding features are extracted and instructed as training and testing data.

Training data is used to train the ID3 classifier

Testing data is used for validating trained classifier by training set.

In this paper the features are invariant moments and the classifier is ID3. Hence the proposed classifier named as in short IVMID3.

The following fig 7, 8 & 9 explains the building process of proposed methodology IVMID3.

Building a IVMID3 classifier using the training data set of images is given in fig7



The validation steps of the IVMID3 is given in flow chart below. Testing data is used for validating trained classifier IVMID3



Face Recognition of a questioned image can be obtained by following steps as given in the following flow chart.



The Mean, Standard Deviation, CV of 10 features from 455 images are computed and listed in the following Table VI.

| | Mean | SD | CV | IM1 | IM2 | IM3 | IM4 | IM5 | IM6 | IM7 | class |
|-----|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| | | | | | | | | | | - | |
| Me | 127.359 | 66.2959 | 52.6754 | 0.00136 | 1.36791 | 5.65165 | 5.50912 | 3.92157 | 1.44788 | 5.21998 | 479.582 |
| an | 3933 | 909 | 2088 | 06 | E-07 | E-11 | E-11 | E-21 | E-14 | E-21 | 0225 |
| | 14.6052 | 6.54152 | 7.59627 | 0.00016 | 6.38067 | 8.08688 | 7.70735 | 3.11547 | 3.14213 | 3.25518 | 227.076 |
| Std | 4582 | 8751 | 4292 | 3257 | E-08 | E-11 | E-11 | E-20 | E-14 | E-20 | 7236 |
| | | | | | | | | | | - | |
| | 11.4677 | 9.86715 | 14.4209 | 11.9988 | 46.6453 | 143.088 | 139.901 | 794.444 | 217.015 | 623.600 | 47.3488 |
| CV | 4136 | 586 | 0858 | 6664 | 7158 | 8439 | 6765 | 928 | 4216 | 6473 | 8152 |
| | | | | | | | | | | | |

Table VI: Mean, SD, CV of features

After extracting the selected features of the images, the following discretization technique is used.

Lower Integer part of $((x-mean)/\sigma).k)+KK$ is used to discretization of the data of each image.

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With k 7

KK 28

Using above discretization factor a Discretized data of sample data of 10 images is given in Table VII

| D_Mean | D_SD | D_CV | D_IM1 | D_IM2 | D_IM3 | D_IM4 | D_IM5 | D_IM6 | D_IM7 | Class |
|--------|------|------|-------|-------|-------|-------|-------|-------|-------|-------|
| 18 | 28 | 36 | 28 | 33 | 25 | 24 | 27 | 23 | 29 | 180 |
| 21 | 26 | 32 | 30 | 19 | 29 | 36 | 30 | 31 | 29 | 260 |
| 40 | 22 | 15 | 18 | 24 | 25 | 26 | 27 | 27 | 28 | 322 |
| 33 | 35 | 28 | 24 | 27 | 23 | 26 | 27 | 24 | 29 | 418 |
| 31 | 34 | 28 | 25 | 27 | 23 | 27 | 26 | 26 | 29 | 449 |
| 35 | 44 | 32 | 18 | 16 | 25 | 27 | 26 | 26 | 28 | 483 |
| 29 | 22 | 22 | 27 | 28 | 26 | 23 | 27 | 25 | 29 | 519 |
| 25 | 22 | 25 | 35 | 38 | 28 | 23 | 27 | 24 | 29 | 660 |
| 31 | 17 | 17 | 21 | 20 | 28 | 27 | 27 | 27 | 28 | 741 |
| 34 | 28 | 22 | 21 | 33 | 30 | 24 | 27 | 26 | 29 | 973 |

Table VII: Discretized data

Where D- Stands for Discretization, IM- Invariant Moment

Rough sets theory provides a novel approach to knowledge description and to approximation of sets. In rough sets theory, feature values of sample objects are collected in what are known as information tables. Rows of such a table correspond to objects and columns correspond to object features. Rough set theory provides a mathematical tool that can be used for both feature selection and knowledge discovery. It helps us to find out the minimal attribute sets called 'Reduct' to classify objects without deterioration of classification quality

Table VIII: Reduct computation

| Reduct | Mean | SD | IMV6 | IMV2 | IMV4 |
|--------|-------------|-------------|-------------|-------------|------|
| Kapas | 0.193258427 | 0.948314607 | 0.993258427 | 0.995505618 | 1 |
| | | | | | |
| А | 445 | 359 | 23 | 3 | 2 |
| | | | | | |
| Time | 0.096713079 | | | | |

The Reduct is Mean, SD, IM6, IM2 and IM4

Reduced discretization Table IX of 10 images is as follows

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| Mean | SD | IMV6 | IMV2 | IMV4 | Class |
|------|----|------|------|------|-------|
| 18 | 28 | 23 | 33 | 24 | 180 |
| 21 | 26 | 31 | 19 | 36 | 260 |
| 40 | 22 | 27 | 24 | 26 | 322 |
| 33 | 35 | 24 | 27 | 26 | 418 |
| 31 | 34 | 26 | 27 | 27 | 449 |
| 35 | 44 | 26 | 16 | 27 | 483 |
| 29 | 22 | 25 | 28 | 23 | 519 |
| 25 | 22 | 24 | 38 | 23 | 660 |
| 31 | 17 | 27 | 20 | 27 | 741 |
| 34 | 28 | 26 | 33 | 24 | 973 |

Table IX: Reduct of discretized data

ID3 algorithm invented by Ross Quinlan [8] which is used to generate a decision tree from a dataset. Using Matlab, the code of the following algorithm ID3 decision tree has been built

The ID3 decision tree for the Bio id face bench mark data is as follows

% id3tree for data set =Bio Sampled Reduct

```
function classify = f_id3tree_BioSample_Reduct(data)
D_{mean} = data(1);
switch D_mean
  case 9
    classify = 322;
  case 10
    classify = 322;
  case 11
    classify = 322;
  case 13
    classify = 322;
  case 14
    classify = 322;
  case 15
    classify = 660;
  case 16
    D_std = data(2);
    switch D_std
       case 17
         classify = 660;
```

case 20

```
classify = 322;
     otherwise classify = 999; % default case
  end
case 17
  classify = 322;
case 18
  D_std = data(2);
  switch D_std
     case 23
       classify = 322;
     case 24
       classify = 322;
     case 25
       classify = 322;
     case 27
       classify = 180;
     case 28
       classify = 180;
     case 29
       classify = 180;
     case 31
       classify = 180;
     otherwise classify = 999; % default case
  end
case 19
  D_std = data(2);
  switch D_std
     case 24
       classify = 180;
     case 25
       classify = 260;
     case 29
       classify = 180;
     case 30
       classify = 180;
     case 31
       classify = 180;
     case 36
       classify = 322;
     otherwise classify = 999; % default case
  end
case 20
```

```
D_std = data(2);
  switch D_std
     case 24
       classify = 260;
     case 25
       classify = 260;
     case 26
       classify = 260;
     case 36
       classify = 322;
     otherwise classify = 999; % default case
  end
case 21
  D_std = data(2);
  switch D_std
     case 26
       classify = 260;
     case 42
       classify = 322;
     otherwise classify = 999; % default case
  end
case 22
  classify = 322;
case 23
  D_std = data(2);
  switch D_std
     case 17
       classify = 260;
     case 28
       classify = 973;
     case 41
       classify = 322;
     case 47
       classify = 322;
     otherwise classify = 999; % default case
  end
case 24
  classify = 973;
case 25
  D_std = data(2);
  switch D_std
     case 22
```

```
classify = 660;
     case 23
       classify = 660;
     case 29
       classify = 973;
     case 30
       classify = 973;
     case 31
       classify = 973;
     otherwise classify = 999; % default case
  end
case 26
  D_std = data(2);
  switch D_std
     case 22
       classify = 660;
     case 23
       classify = 660;
     case 30
       classify = 973;
     case 31
       classify = 973;
     case 32
       classify = 973;
     otherwise classify = 999; % default case
  end
case 27
  D_std = data(2);
  switch D_std
     case 21
       classify = 260;
     case 22
       classify = 260;
     case 29
       classify = 973;
     case 32
       classify = 973;
     otherwise classify = 999; % default case
  end
case 28
  classify = 260;
case 29
```

```
D_std = data(2);
  switch D_std
     case 16
       classify = 741;
     case 17
       classify = 741;
     case 23
       classify = 519;
     case 24
       classify = 519;
     otherwise classify = 999; % default case
  end
case 30
  D_std = data(2);
  switch D_std
     case 17
       classify = 741;
     case 18
       classify = 741;
     case 24
       classify = 519;
     case 25
       classify = 519;
     case 35
       classify = 322;
     case 36
       classify = 322;
     otherwise classify = 999; % default case
  end
case 31
  D_IM2 = data(4);
  switch D_IM2
     case 19
       classify = 741;
     case 20
       classify = 741;
     case 25
       classify = 519;
     case 26
       classify = 483;
     case 27
       classify = 449;
```

```
case 28
       classify = 449;
     case 29
       classify = 322;
     case 30
       classify = 418;
     case 32
       classify = 418;
     otherwise classify = 999; % default case
  end
case 32
  D_std = data(2);
  switch D_std
     case 17
       classify = 260;
     case 18
       D_IM6 = data(3);
       switch D_IM6
         case 25
            classify = 260;
         case 26
            classify = 741;
         otherwise classify = 999; % default case
       end
     case 19
       classify = 260;
    case 20
       classify = 260;
     case 28
       classify = 322;
     case 29
       classify = 418;
     case 30
       classify = 418;
     case 31
       classify = 418;
     case 32
       classify = 449;
     case 33
       D_IM6 = data(3);
       switch D_IM6
          case 24
```

```
D_IM2 = data(4);
            switch D_IM2
              case 27
                 classify = 449;
              case 28
                 classify = 418; % majority voting
              otherwise classify = 999; % default case
            end
         case 25
            classify = 449;
         case 26
            classify = 418;
         otherwise classify = 999; % default case
       end
     case 36
       classify = 322;
     case 37
       classify = 322;
     otherwise classify = 999; % default case
  end
case 33
  D_std = data(2);
  switch D_std
     case 18
       classify = 260;
     case 19
       classify = 260;
     case 28
       classify = 322;
     case 29
       classify = 322;
     case 30
       classify = 418;
     case 31
       D_IM6 = data(3);
       switch D_IM6
         case 24
            classify = 418;
         case 25
            classify = 418;
         case 26
            classify = 418;
```

case 30

```
classify = 322;
         otherwise classify = 999; % default case
       end
     case 32
       classify = 418;
     case 33
       classify = 322;
     otherwise classify = 999; % default case
  end
case 34
  D_std = data(2);
  switch D_std
     case 19
       classify = 260;
     case 28
       classify = 973;
     case 29
       classify = 322;
     case 30
       classify = 449;
     case 32
       classify = 418;
     case 33
       classify = 418;
     case 35
       D_IM6 = data(3);
       switch D_IM6
         case 24
            classify = 449;
         case 25
            classify = 449;
         case 26
            classify = 322;
         otherwise classify = 999; % default case
       end
     case 36
       classify = 322;
     case 37
       classify = 483;
     case 38
       classify = 483;
```

```
case 46
          classify = 483;
       case 48
          classify = 483;
       otherwise classify = 999; % default case
     end
  case 35
     classify = 483;
  case 36
     classify = 483;
  case 37
     classify = 322;
  case 38
     classify = 973;
  case 39
     classify = 322;
  case 40
    classify = 322;
  otherwise classify = 999; % default case
end
```

A 10-fold validation on the reduced discretised data is given in below Table X.

Tables: X On Reduced Discretized

| fold | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | mean | SD | CV |
|------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|------|------|
| ID3 | 91.11 | 88.89 | 95.56 | 97.78 | 88.89 | 95.56 | 95.56 | 97.78 | 95.56 | 92.50 | 93.92 | 3.35 | 3.57 |

4. CONCLUSIONS

A same ID3 builder is also carried on discretized data without dimension reduction. The performance is very low for this bench mark data Whereas Reduced data is giving significantly high performance on this bench mark data around 91% This study reveals with 5 dimensional features are sufficient for face recognition system.

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Table II: Features of the images given in Fig 3

| IS | S_ | Ν | Ν | m | m | | | | | | | | | | | cla |
|----|----|---|---|----|----|-------|-------|-------|-------|-------|-------|------|-------|-------|-------|-----|
| No | id | R | С | in | ax | mean | SD | CV | IM1 | IM2 | IM3 | IM4 | IM5 | IM6 | IM7 | SS |
| | | 2 | 3 | | | | | | | | | | | | | |
| | 18 | 8 | 8 | | 25 | 107.5 | 67.10 | 62.41 | 0.001 | 1.84 | 2.39 | 1.41 | 1.63 | -6E- | 3.91 | 18 |
| 1 | 0 | 6 | 4 | 0 | 5 | 078 | 222 | 611 | 377 | E-07 | E-11 | E-11 | E-22 | 15 | E-23 | 0 |
| | | 2 | 3 | | | | | | | | | | | | | |
| | 26 | 8 | 8 | | 25 | 113.6 | 64.99 | 57.18 | 0.001 | 5.65 | 7.49 | 1.44 | 1.45 | 3.11 | 8.53 | 26 |
| 43 | 0 | 6 | 4 | 0 | 5 | 477 | 283 | 797 | 417 | E-08 | E-11 | E-10 | E-20 | E-14 | E-22 | 0 |
| | | 2 | 3 | | | | | | | | | | | | - | |
| | 32 | 8 | 8 | 2 | 25 | 154.3 | 60.80 | 39.39 | 0.001 | 1.08 | 2.82 | 3.47 | 2.71 | 1.01 | 1.2E- | 32 |
| 91 | 2 | 6 | 4 | 7 | 5 | 289 | 314 | 841 | 142 | E-07 | E-11 | E-11 | E-22 | E-14 | 21 | 2 |
| | | 2 | 3 | | | | | | | | | | - | - | | |
| 18 | 41 | 8 | 8 | | 25 | 138.5 | 73.16 | 52.80 | 0.001 | 1.34 | 3.01 | 4.07 | 4.1E- | 2.6E- | 1.77 | 41 |
| 3 | 8 | 6 | 4 | 0 | 5 | 516 | 693 | 844 | 27 | E-07 | E-12 | E-11 | 22 | 15 | E-21 | 8 |
| | | 2 | 3 | | | | | | | | | | | | | |
| 21 | 44 | 8 | 8 | | 25 | 135.5 | 72.46 | 53.46 | 0.001 | 1.29 | 4.37 | 4.65 | -2E- | 6.39 | 1.37 | 44 |
| 4 | 9 | 6 | 4 | 0 | 5 | 407 | 299 | 215 | 298 | E-07 | E-12 | E-11 | 21 | E-15 | E-21 | 9 |
| | | 2 | 3 | | | | | | | | | | - | | - | |
| 24 | 48 | 8 | 8 | | 25 | 143.2 | 82.13 | 57.35 | 0.001 | 3.2E- | 2.2E- | 5.43 | 2.8E- | 7.96 | 8.6E- | 48 |
| 7 | 3 | 6 | 4 | 0 | 5 | 14 | 398 | 054 | 14 | 08 | 11 | E-11 | 21 | E-15 | 22 | 3 |
| | | 2 | 3 | | | | | | | | | | - | | - | |
| 28 | 51 | 8 | 8 | | 25 | 131.3 | 61.39 | 46.72 | 0.001 | 1.4E- | 3.51 | 8.39 | 4.4E- | 2.88 | 3.8E- | 51 |
| 3 | 9 | 6 | 4 | 0 | 5 | 982 | 059 | 101 | 359 | 07 | E-11 | E-12 | 23 | E-15 | 23 | 9 |
| | | 2 | 3 | | | | | | | | | | - | | | |
| 32 | 66 | 8 | 8 | | 25 | 122.4 | 61.04 | 49.86 | 0.001 | 2.36 | 6.64 | 4.25 | 5.5E- | 6.13 | 1.79 | 66 |
| 0 | 0 | 6 | 4 | 0 | 5 | 23 | 817 | 656 | 533 | E-07 | E-11 | E-12 | 24 | E-16 | E-23 | 0 |
| | | 2 | 3 | | | | | | | | | | | | - | |
| 36 | 74 | 8 | 8 | 1 | 25 | 134.4 | 56.12 | 41.73 | 0.001 | 7.04 | 5.71 | 4.79 | 1.06 | 1.13 | 2.5E- | 74 |
| 6 | 1 | 6 | 4 | 1 | 5 | 783 | 519 | 55 | 198 | E-08 | E-11 | E-11 | E-21 | E-14 | 21 | 1 |
| | | 2 | 3 | | | | | | | | | | | | - | |
| 40 | 97 | 8 | 8 | | 25 | 141.8 | 66.46 | 46.86 | 0.001 | 1.83 | 8.04 | 1.65 | 4.34 | 6.68 | 1.9E- | 97 |
| 4 | 3 | 6 | 4 | 0 | 5 | 279 | 154 | 07 | 216 | E-07 | E-11 | E-11 | E-22 | E-15 | 22 | 3 |

| | | | | Aver- | | Aver- | Aver- | Aver- | | Aver- | |
|------|---|----------|---------|---------|----------|---------|--------|--------|----------|--------|----------|
| S_i | | Average | Average | age of | Average | age of | age of | age of | Average | age of | Average |
| d | # | of mean | of SD | cv | of IM1 | IM2 | IM3 | IM4 | of IM5 | IM6 | of IM7 |
| | | | | | | | | | - | | - |
| | 4 | 107.8923 | 66.6817 | 61.8027 | 0.001406 | 1.62381 | 7.0521 | 6.6784 | 2.99866E | 8.7601 | 3.29988 |
| 180 | 2 | 299 | 7405 | 5916 | 273 | E-07 | 3E-11 | E-11 | -21 | 5E-15 | E-21 |
| | 4 | 126.0425 | 61.0776 | 49.1227 | 0.001300 | 6.44151 | 5.3265 | 6.7843 | 5.02982E | 1.3946 | 2.15414 |
| 260 | 8 | 167 | 4908 | 703 | 714 | E-08 | 5E-11 | 8E-11 | -21 | 2E-14 | E-21 |
| | | | | | | | | | | | - |
| | 9 | 127.4163 | 70.0131 | 56.4513 | 0.001390 | 1.6056 | 1.0035 | 1.2674 | 1.82485E | 4.7229 | 2.3999E- |
| 322 | 2 | 091 | 882 | 1684 | 854 | E-07 | 4E-10 | 7E-10 | -20 | 5E-14 | 20 |
| | | | | | | | | | - | | |
| | 3 | 138.1173 | 69.7933 | 50.5347 | 0.001313 | 1.58056 | 1.1362 | 3.4912 | 9.8822E- | 1.7506 | 4.52984 |
| 418 | 1 | 217 | 661 | 8523 | 717 | E-07 | 9E-11 | 7E-11 | 22 | 5E-15 | E-22 |
| | | | | | | | | | - | | |
| | 3 | 139.9084 | 69.9805 | 50.0389 | 0.001246 | 8.87394 | 1.5516 | 2.3163 | 4.17611E | 2.0090 | 4.00224 |
| 449 | 3 | 734 | 0072 | 4005 | 47 | E-08 | 9E-11 | 2E-11 | -22 | 3E-15 | E-22 |
| | | | | | | | | | - | | - |
| | 3 | 142.5492 | 76.9256 | 53.9817 | 0.001266 | 7.64848 | 2.2399 | 4.5745 | 1.86136E | 7.925E | 6.19209 |
| 483 | 6 | 677 | 5848 | 6995 | 475 | E-08 | 2E-11 | E-11 | -21 | -15 | E-22 |
| | | | | | | | | | - | | - |
| | 3 | 132.9486 | 63.0344 | 47.4123 | 0.001331 | 1.16865 | 3.5038 | 6.9853 | 4.81473E | 1.977E | 3.73271 |
| 519 | 7 | 781 | 515 | 1889 | 525 | E-07 | E-11 | 5E-12 | -23 | -15 | E-23 |
| | 4 | 112.0124 | 58.6750 | 52.6236 | 0.001654 | 2.33206 | 7.1007 | 1.0068 | 1.93599E | 3.8954 | 2.69373 |
| 660 | 6 | 274 | 1109 | 2422 | 063 | E-07 | 6E-11 | 9E-11 | -22 | 8E-15 | E-22 |
| | | | | | | | | | | | - |
| | 3 | 132.4420 | 56.6239 | 42.7562 | 0.001215 | 6.82216 | 6.0748 | 5.0381 | 1.69671E | 1.2042 | 2.54219 |
| 741 | 8 | 561 | 8146 | 7727 | 22 | E-08 | 9E-11 | 1E-11 | -21 | 5E-14 | E-21 |
| | | | | | | | | | - | - | |
| | 4 | 124.6726 | 69.1149 | 55.5367 | 0.001357 | 1.89596 | 4.4207 | 1.5804 | 2.24356E | 1.3143 | 2.02166 |
| 973 | 2 | 149 | 9711 | 6556 | 795 | E-07 | 2E-11 | 1E-11 | -22 | 8E-15 | E-23 |
| (bla | | | | | | | | | | | |
| nk) | | | | | | | | | | | |
| Gra | | | | | | | | | | | |
| nd | 4 | | | | | | | | | | - |
| To- | 4 | 127.3593 | 66.2959 | 52.6754 | 0.001360 | 1.36791 | 5.6516 | 5.5091 | 3.92157E | 1.4478 | 5.21998 |
| tal | 5 | 933 | 909 | 2088 | 6 | E-07 | 5E-11 | 2E-11 | -21 | 8E-14 | E-21 |

Table IV: Averages of the Features of the images of the considered Data Set

| S_i | | SD of | SD of | SD of | SD of | SD of | SD of | SD of | SD of | SD of | SD of |
|-----|----|---------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| d | # | mean | SD | CV | IM1 | IM2 | IM3 | IM4 | IM5 | IM6 | IM7 |
| | | 0.82453 | 1.1503 | 0.8644 | 2.8086 | 2.1197 | 2.8386 | 2.5222 | 1.4703 | 8.4911 | 3.7317 |
| 180 | 42 | 3435 | 98815 | 60715 | 5E-05 | 3E-08 | 5E-11 | 6E-11 | 3E-21 | 8E-15 | 3E-21 |
| | | 12.1440 | 3.0461 | 7.1277 | 0.0001 | 2.0233 | 2.3981 | 4.8339 | 5.4081 | 1.1193 | 3.3284 |
| 260 | 48 | 3886 | 82802 | 12865 | 2223 | 4E-08 | 5E-11 | 4E-11 | 4E-21 | 5E-14 | E-21 |
| | | 19.6036 | 6.0440 | 11.167 | 0.0002 | 6.5749 | 1.6352 | 1.3702 | 6.6610 | 5.6848 | 6.8542 |
| 322 | 92 | 2721 | 78985 | 42099 | 14785 | 7E-08 | 5E-10 | 7E-10 | 2E-20 | 8E-14 | 4E-20 |
| | | 1.61442 | 1.4090 | 1.0017 | 2.3953 | 1.5069 | 5.4569 | 6.4639 | 6.0039 | 3.2782 | 5.2999 |
| 418 | 31 | 2904 | 36464 | 79154 | 9E-05 | 4E-08 | 5E-12 | 8E-12 | 6E-22 | 8E-15 | E-22 |
| | | 2.15126 | 1.7502 | 1.7521 | 3.7608 | 2.8347 | 6.7604 | 8.6748 | 3.2944 | 1.2591 | 4.9568 |
| 449 | 33 | 5997 | 9161 | 43468 | 8E-05 | 3E-08 | 7E-12 | 3E-12 | 4E-22 | 9E-15 | 7E-22 |
| | | 1.67953 | 2.3023 | 2.0658 | 4.6672 | 1.7178 | 7.1987 | 8.4290 | 7.4939 | 2.0467 | 3.2887 |
| 483 | 36 | 0631 | 96832 | 28019 | 9E-05 | 3E-08 | E-12 | 4E-12 | 8E-22 | 8E-15 | 5E-22 |
| | | 0.70992 | 0.4988 | 0.2184 | 1.1089 | 8.0226 | 2.9509 | 3.6061 | 3.5937 | 1.3486 | 3.0070 |
| 519 | 37 | 8523 | 78652 | 64273 | 5E-05 | 7E-09 | 3E-12 | 7E-12 | 9E-23 | 1E-15 | 4E-23 |
| | | 10.4871 | 2.5765 | 2.6528 | 0.0001 | 1.1651 | 1.4047 | 8.7446 | 2.9167 | 3.8255 | 3.3209 |
| 660 | 46 | 6471 | 02386 | 43016 | 19239 | 9E-08 | 1E-11 | 2E-12 | 6E-22 | 1E-15 | 6E-22 |
| | | 1.72926 | 0.6973 | 0.4290 | 2.4665 | 3.1965 | 1.1305 | 6.0251 | 8.9156 | 1.9872 | 4.7087 |
| 741 | 38 | 3129 | 34405 | 5652 | 3E-05 | 4E-09 | 7E-11 | 7E-12 | 2E-22 | 1E-15 | 9E-22 |
| | | 4.96616 | 1.4208 | 2.6740 | 5.8137 | 2.9134 | 1.7252 | 6.3567 | 2.7087 | 3.9171 | 4.0405 |
| 973 | 42 | 4976 | 85015 | 78596 | 3E-05 | 1E-08 | 9E-11 | 8E-12 | 4E-22 | 2E-15 | 4E-22 |
| Gra | | | | | | | | | | | |
| nd | | | | | | | | | | | |
| To- | 44 | 14.6052 | 6.5415 | 7.5962 | 0.0001 | 6.3806 | 8.0868 | 7.7073 | 3.1154 | 3.1421 | 3.2551 |
| tal | 5 | 4583 | 28751 | 74292 | 63257 | 7E-08 | 7E-11 | 5E-11 | 7E-20 | 3E-14 | 8E-20 |

Table V: Standard deviation of the Features of the images of the considered Data Set